# **Beyond the Standard Proton**

for Jefferson Lab, October 2022



James Moore, University of Cambridge





### Talk overview

1. PDFs: a lightning introduction

2. PDF fitting

3. Joint PDF-SMEFT fits

4. The dark side of the proton

# 1. - PDFs: a lightning introduction

# Hadron structure through PDFs

 Hadrons are QCD bound states - they are strongly-coupled, nonperturbative objects.

$$\mathcal{L} = -\frac{1}{4}G^a_{\mu\nu}G^{a,\mu\nu} + \sum_q \overline{q}(i\gamma_\mu D^\mu - m_q)q \longrightarrow \text{hadrons?}$$

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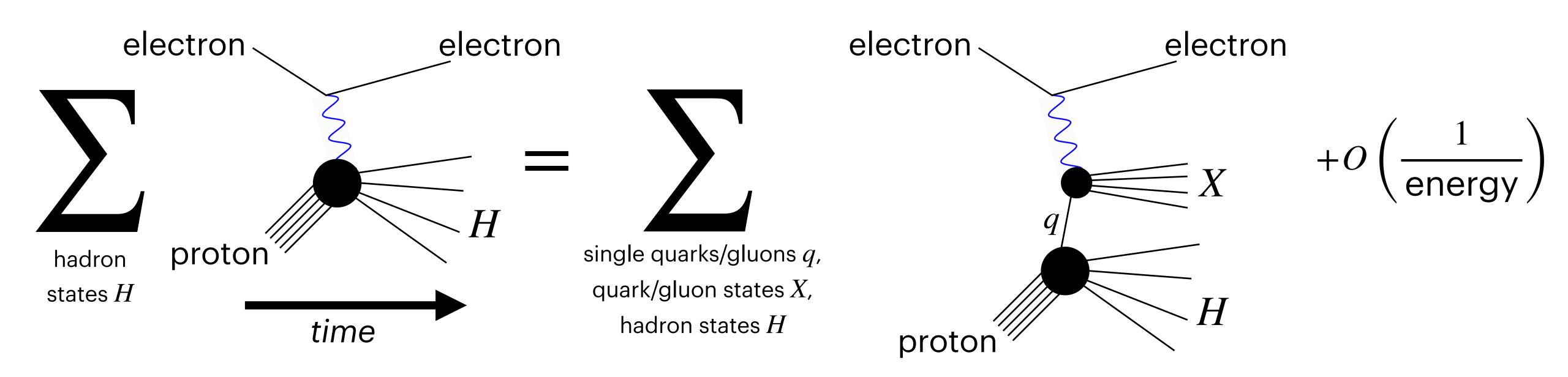
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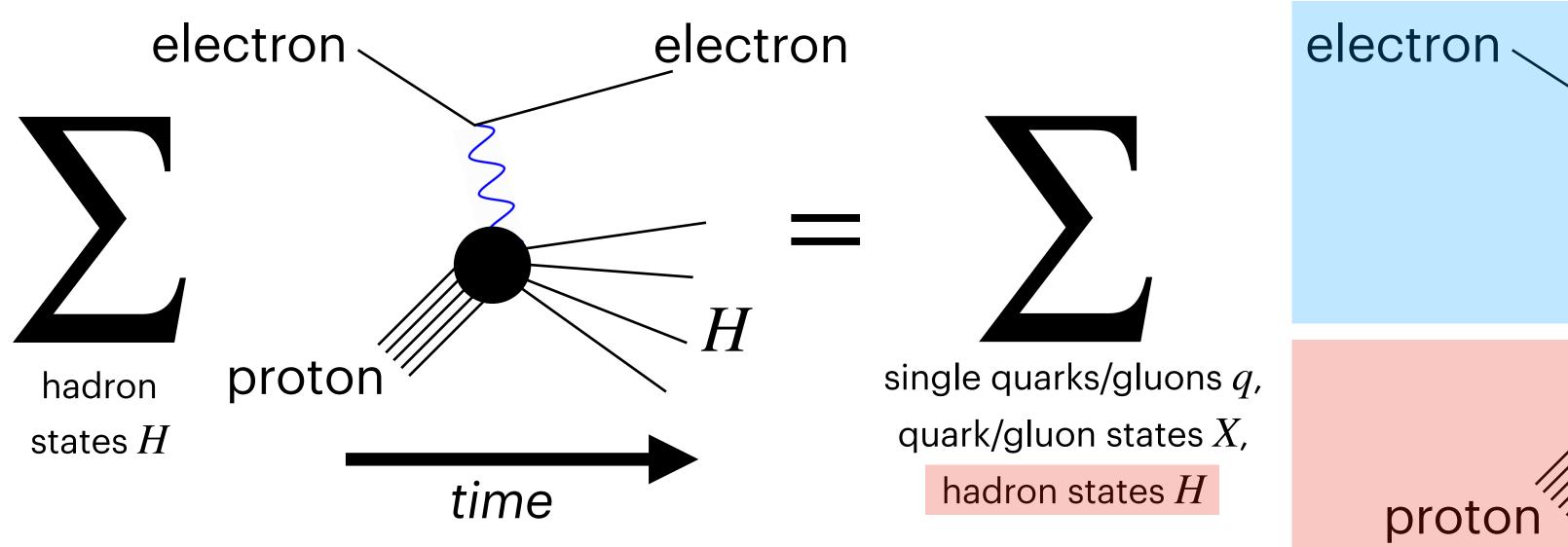
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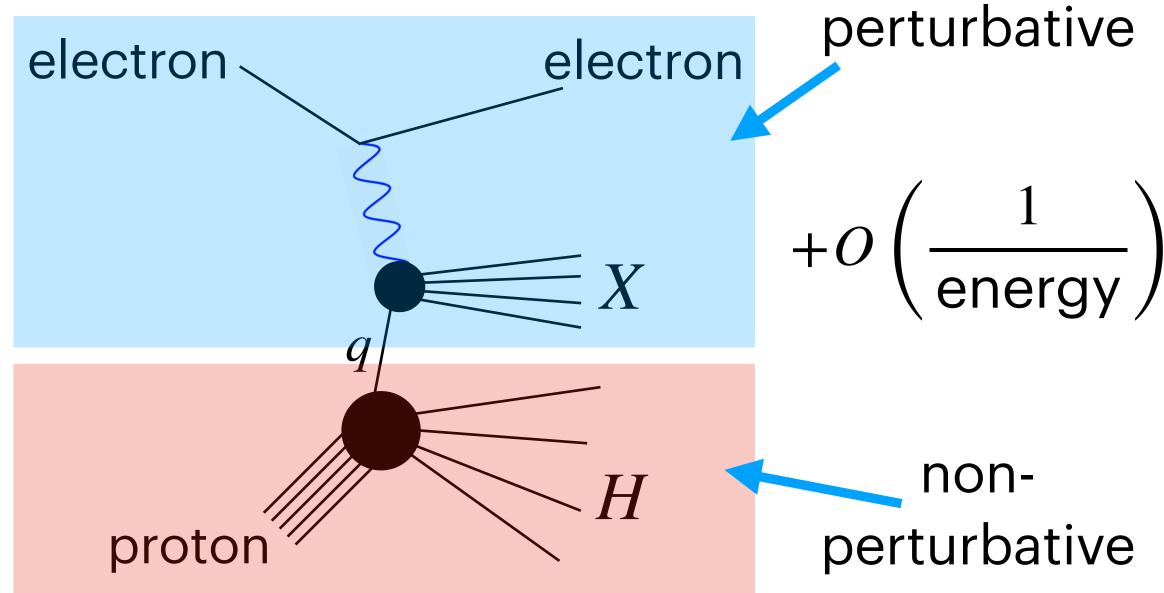
- But we still want to make predictions for experiments involving hadrons!
- **Solution:** package all non-perturbative elements into unknown functions, called **parton distribution functions (PDFs)**.

- This is formalised through factorisation theorems.
- Model case: **deep inelastic scattering**,  $e^-$  + proton  $\rightarrow e^-$  + any hadron.

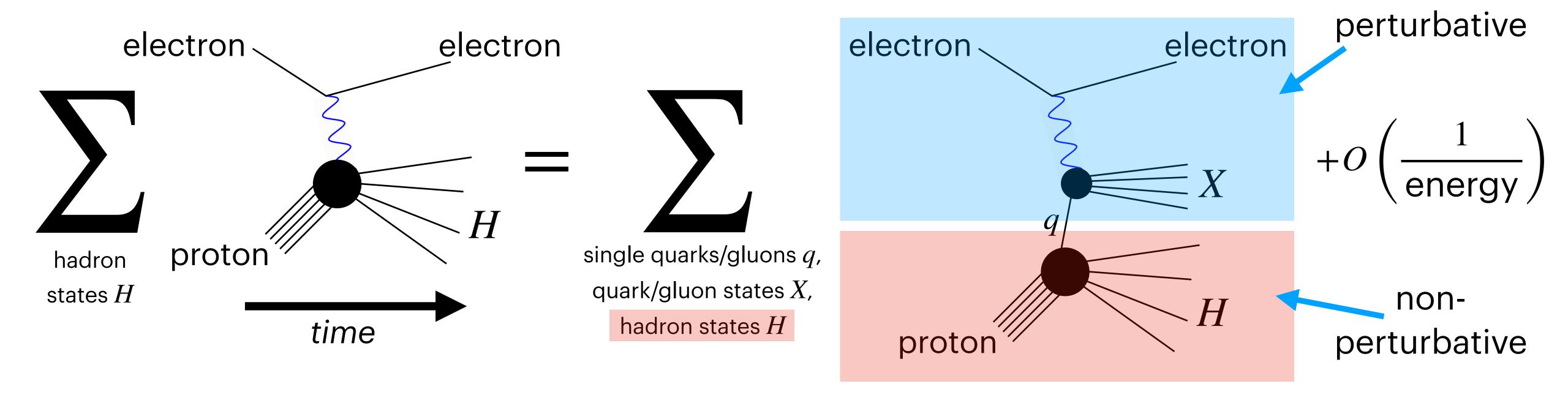


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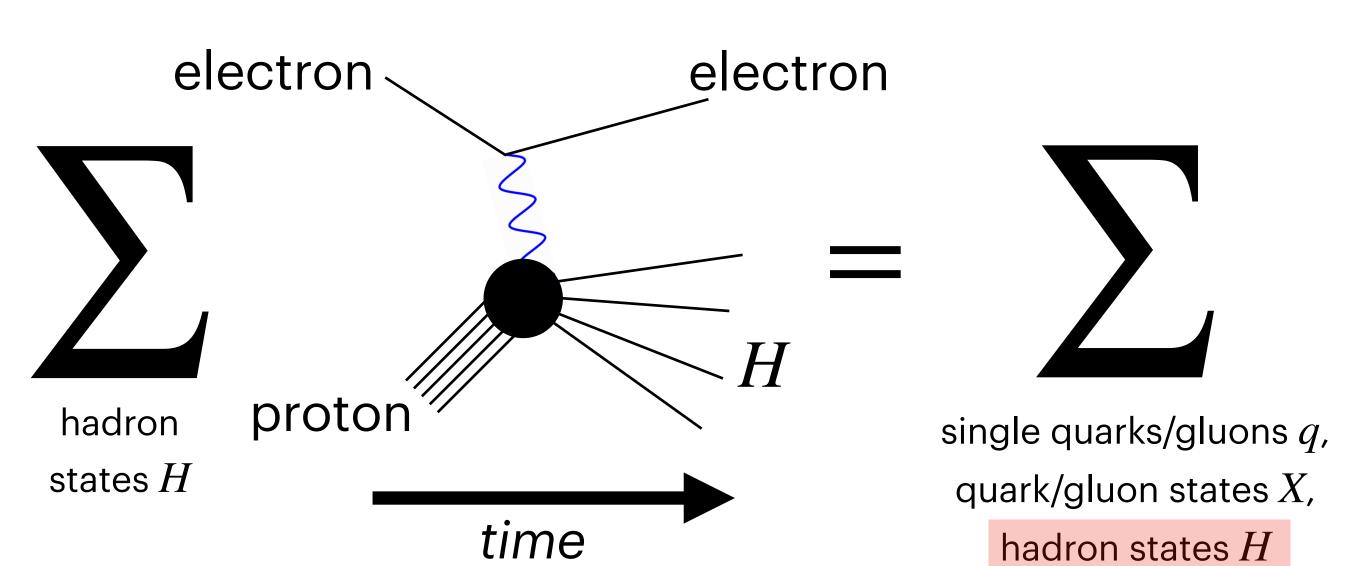


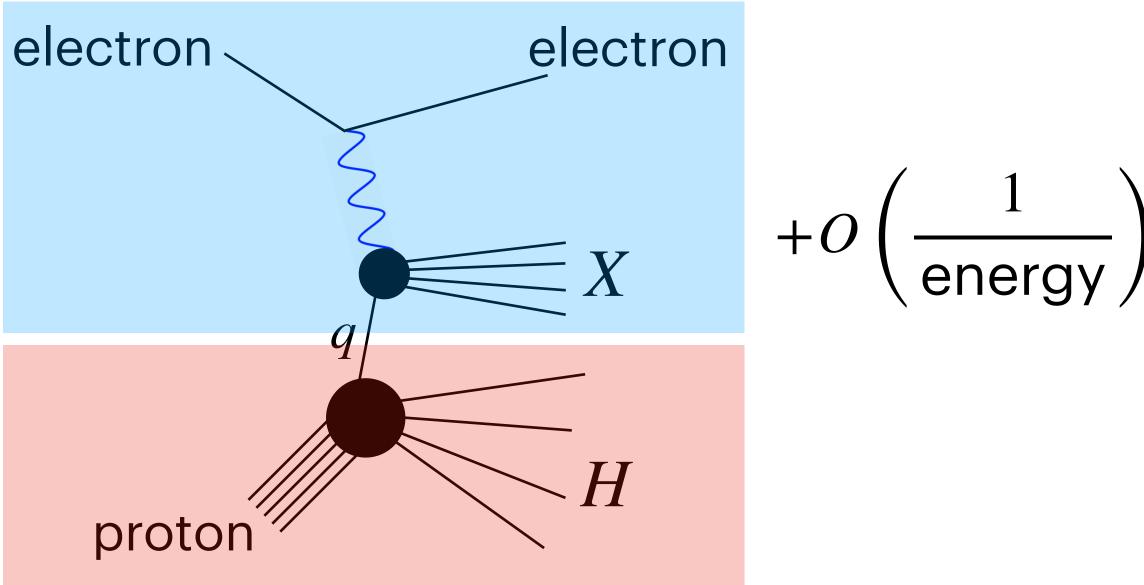


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• The calculation is split into a **perturbative process-dependent part,** and a **non-perturbative, BUT universal, parton distribution function**.





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$$\sigma(x,Q^2) = \sum_{\substack{\text{single quarks/gluons } q, \\ \text{quark/gluon states } X}} \int_{y}^{1} \frac{dy}{\hat{\sigma}_{eq \to eX}} \left(\frac{x}{y},Q^2\right) f_q(y,Q^2) + O\left(\frac{1}{\text{energy}}\right)$$

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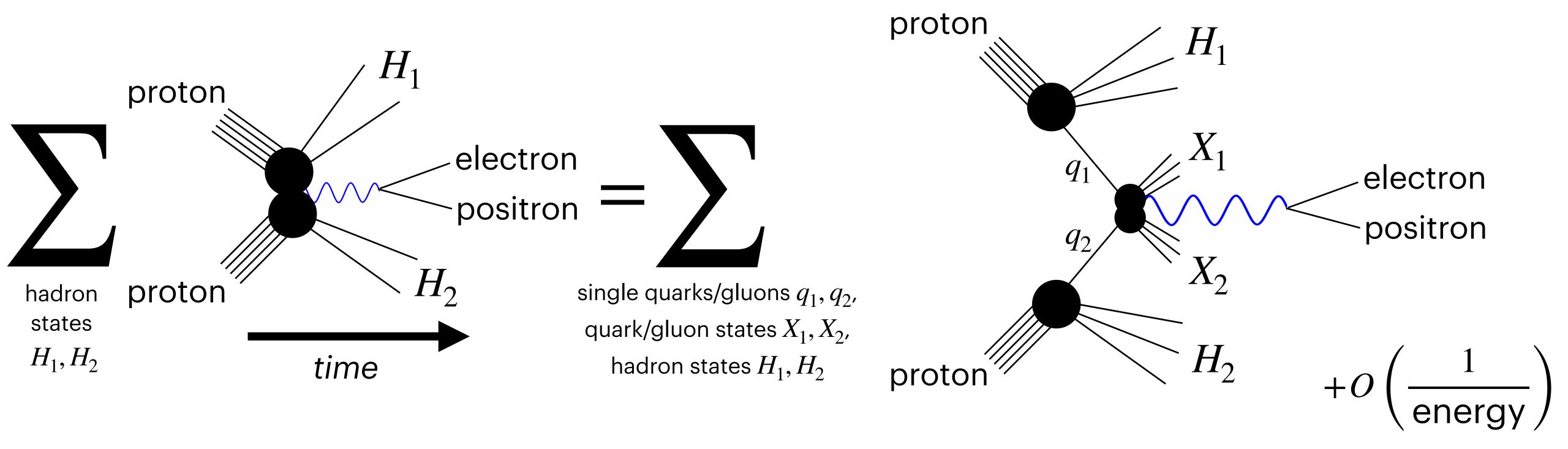
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  - An energy scale  $Q^2$  (comes from absorbing collinear divergences)
  - The fact we are colliding **protons** if we started with a neutron, we would need different PDFs

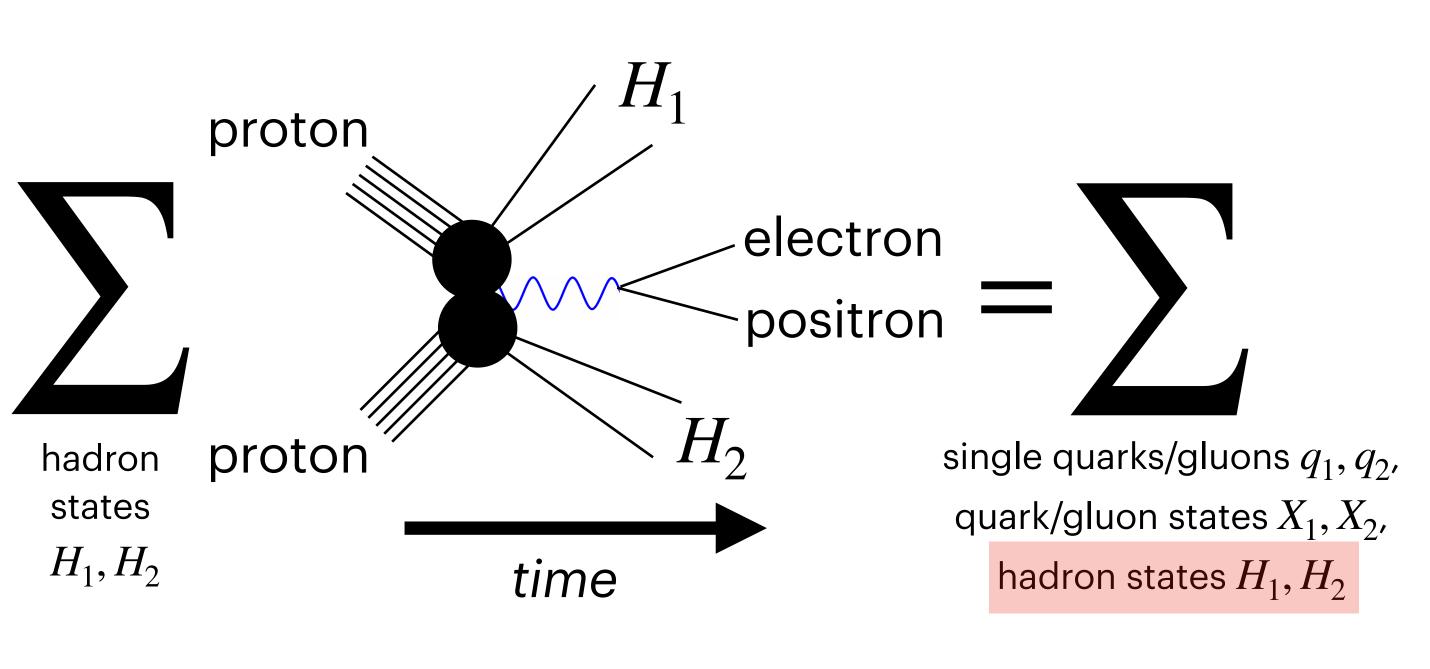
# Universality of PDFs

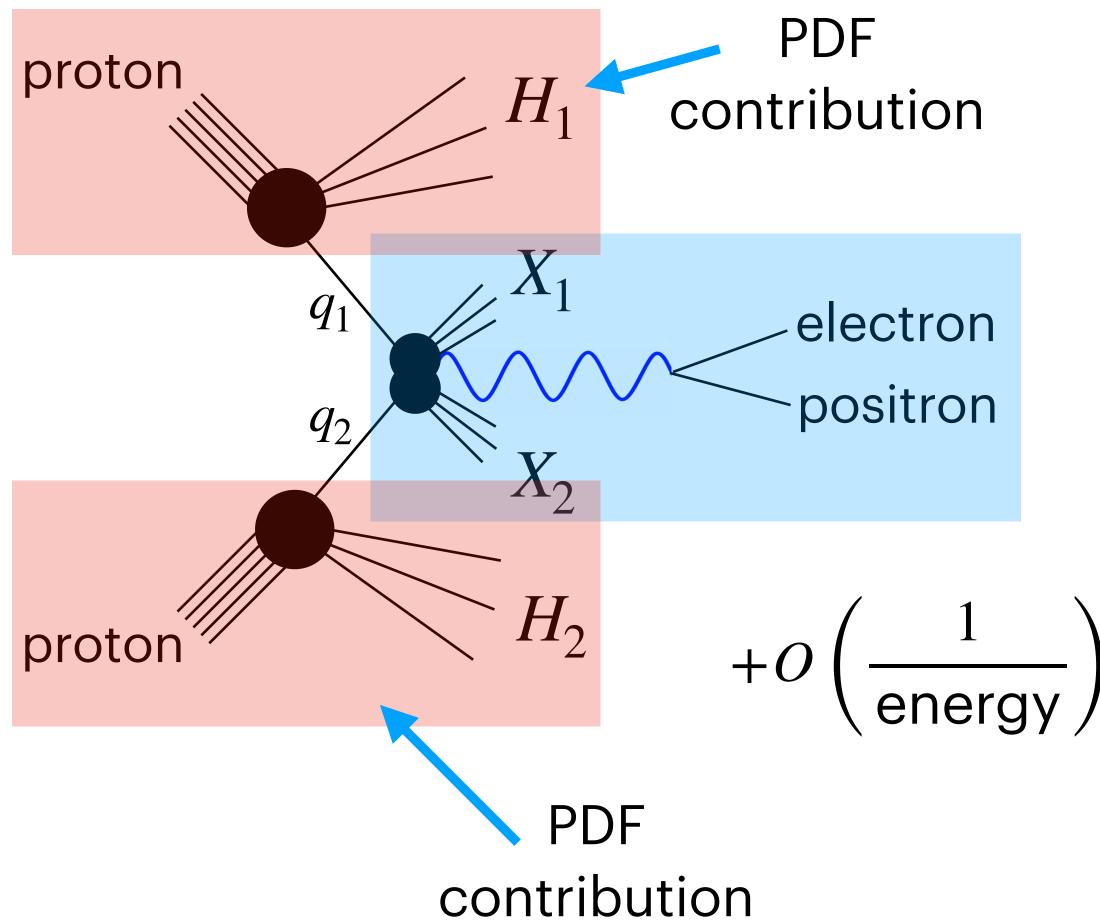
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# Scaling of PDFs

- Whilst the PDFs are non-perturbative, we can still say something about their  $Q^2$ -dependence, which enters the PDFs when we **absorb collinear IR divergences**.
- Just as in **standard UV renormalisation theory**, this leads to a Callan-Symanzik equation for the PDFs called the **DGLAP equation**:

$$Q^{2} \frac{\partial f_{q}(x, Q^{2})}{\partial Q^{2}} = \sum_{\text{quarks/gluons } q'} \int_{x}^{1} \frac{dy}{y} P_{qq'}\left(\frac{x}{y}\right) f_{q'}(x, Q^{2})$$

• The functions (technically distributions)  $P_{qq^\prime}$  are called **splitting functions** and can be determined perturbatively.

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- This means if we know the PDFs at some **initial energy scale**  $Q_0$ , we can compute them at some energy scale  $Q > Q_0$  by solving DGLAP.
- In particular, only the x-dependence of the PDFs is truly unknown.
- We can obtain this x-dependence by fits to collider data, as we shall now describe...

# Summary of PDFs

• The non-perturbative structure of hadrons can be parametrised by parton distribution functions  $f_q(x,Q^2)$ , which depend only on the type of hadron being collided, not on the process.

• The PDFs have known  $Q^2$ -dependence, described by a linear system of integro-differential equations called the **DGLAP** equations.

• The PDFs have **unknown** *x***-dependence**, which must be obtained through fits to experimental data.

# 2. - PDF fitting

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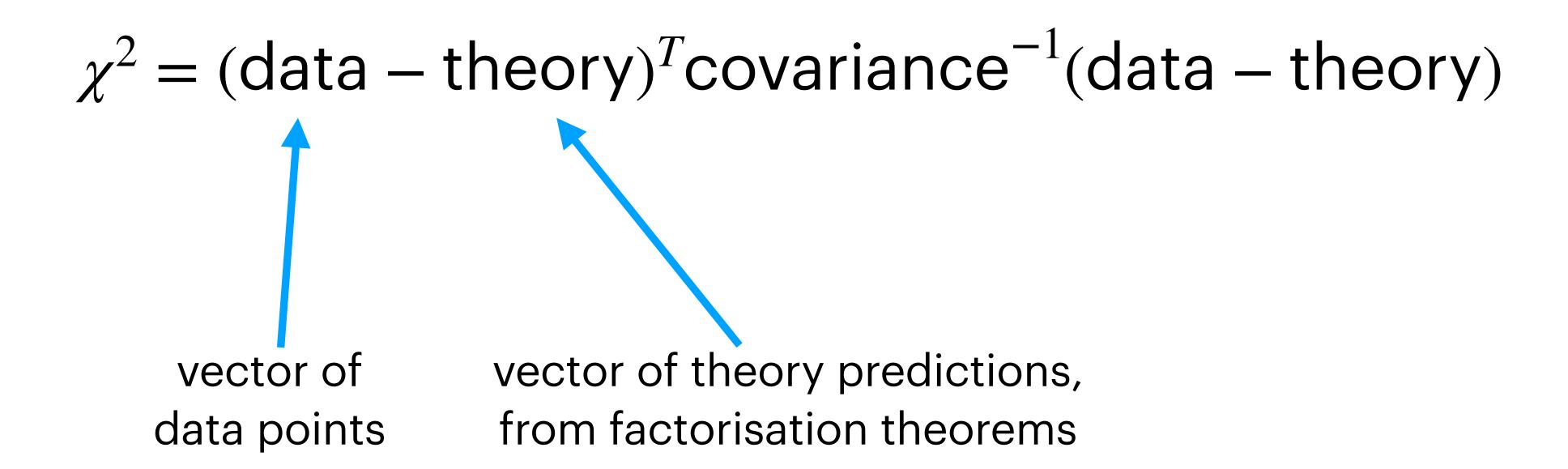
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- Example functional form:

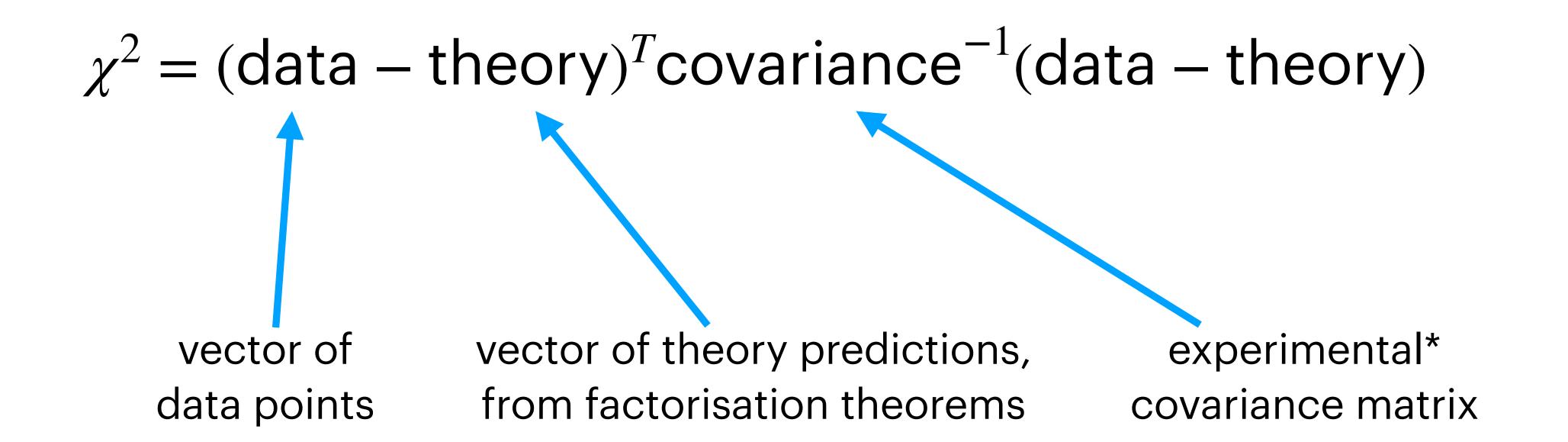
$$f(x,Q_0^2) = Ax^{\alpha}(1-x)^{\beta} \Big(1+ax^{1/2}+bx+cx^{3/2}\Big)$$
 large and small  $x$  behaviour polynomial in  $\sqrt{x}$  motivated by **Regge theory**

$$\chi^2 = (data - theory)^T covariance^{-1}(data - theory)$$

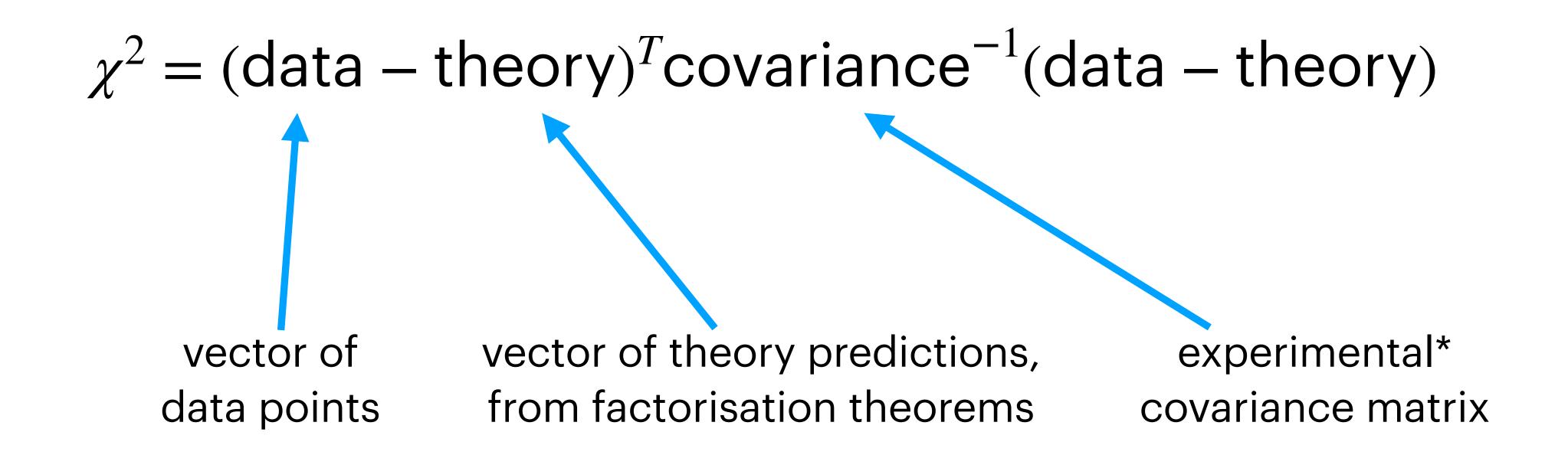
data points

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vector of





• The best-fit parameters are found by **minimising the**  $\chi^2$ -**statistic**, which measures the **goodness of fit** of our model:



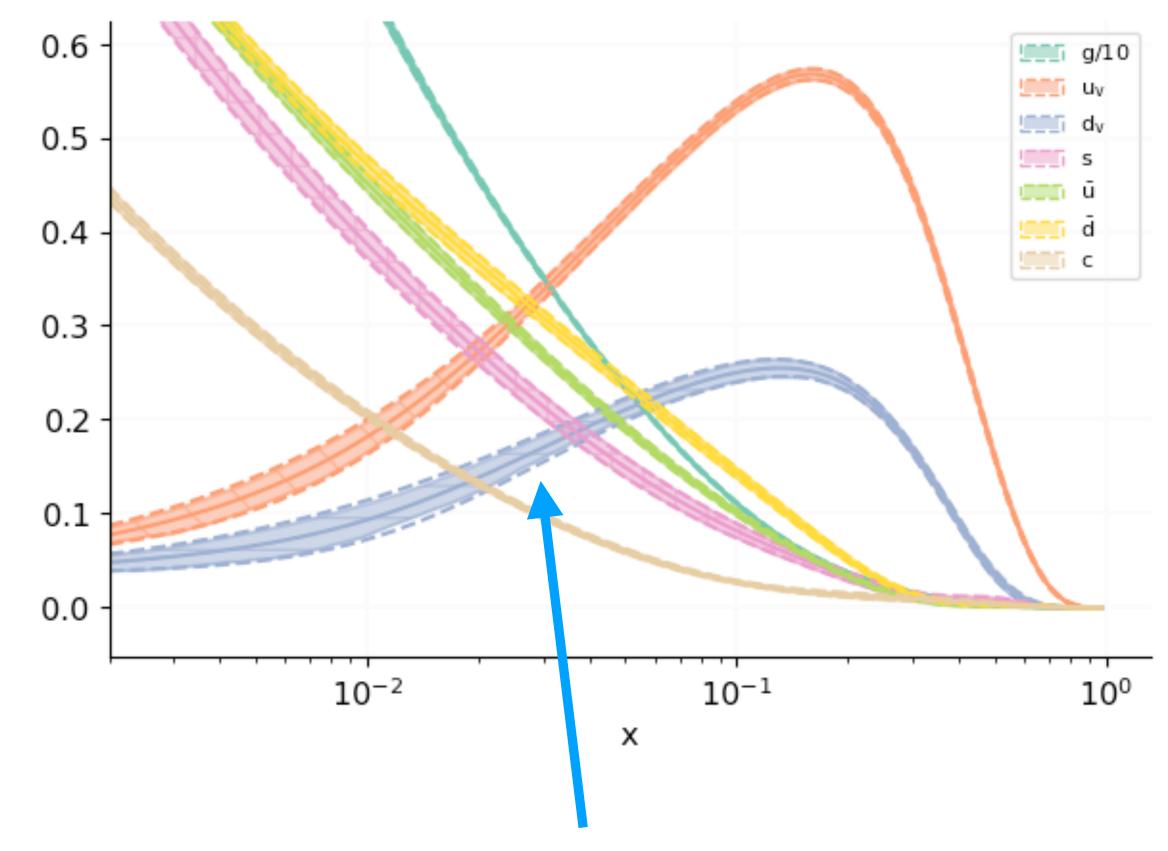
• General idea: we want theory to be close to data, but if the data is more uncertain, we don't require such precise agreement.

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PDFs with error bands

### The choice of functional form

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$$f(x, Q_0^2) = Ax^{\alpha}(1 - x)^{\beta} (1 + ax^{1/2} + bx + cx^{3/2})$$

 This seems a bit arbitrary though! To try to remove as much bias as possible, another possible choice is to parametrise the PDFs using a neural network instead:

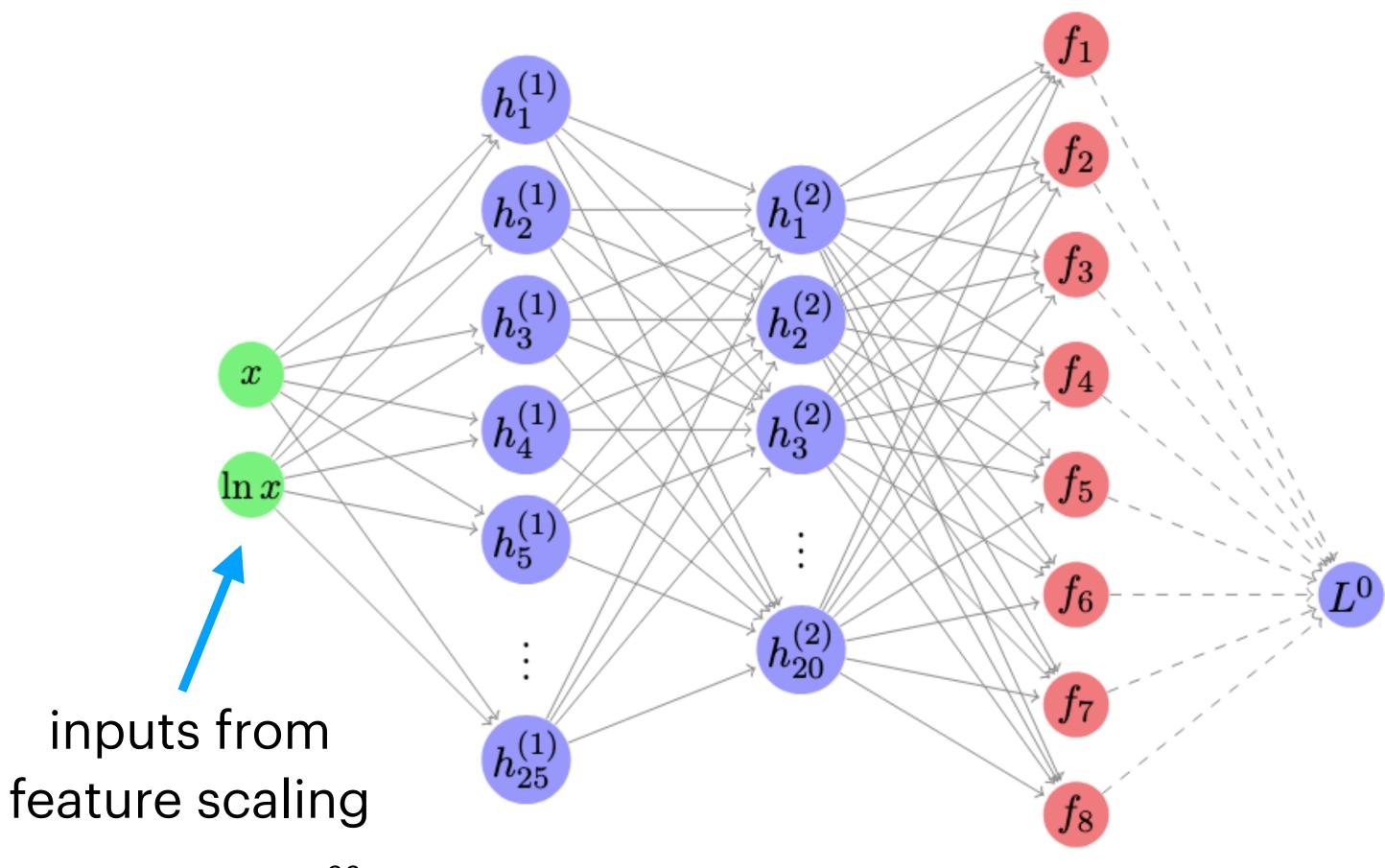
$$f(x, Q_0^2) = Ax^{\alpha}(1 - x)^{\beta}NN(x, \omega)$$

• Here,  $NN(x, \omega)$  is a **neural network** which takes in x as an argument, and has network parameters  $\omega$ .

### The choice of functional form

$$f(x, Q_0^2) = Ax^{\alpha}(1 - x)^{\beta} NN(x, \omega)$$

- The neural network
   parametrisation is
   used by the NNPDF
   collaboration, whose
   fitting code is publicly
   available.
- See 2109.02653 and 2109.02671 for details.



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layer 2

PDF

flavours

Input

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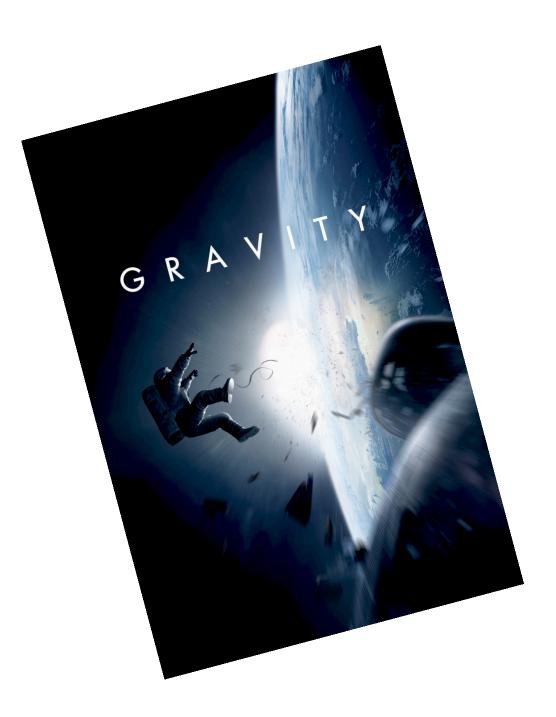
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# 3. - Joint PDF-SMEFT fits

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  - many more...



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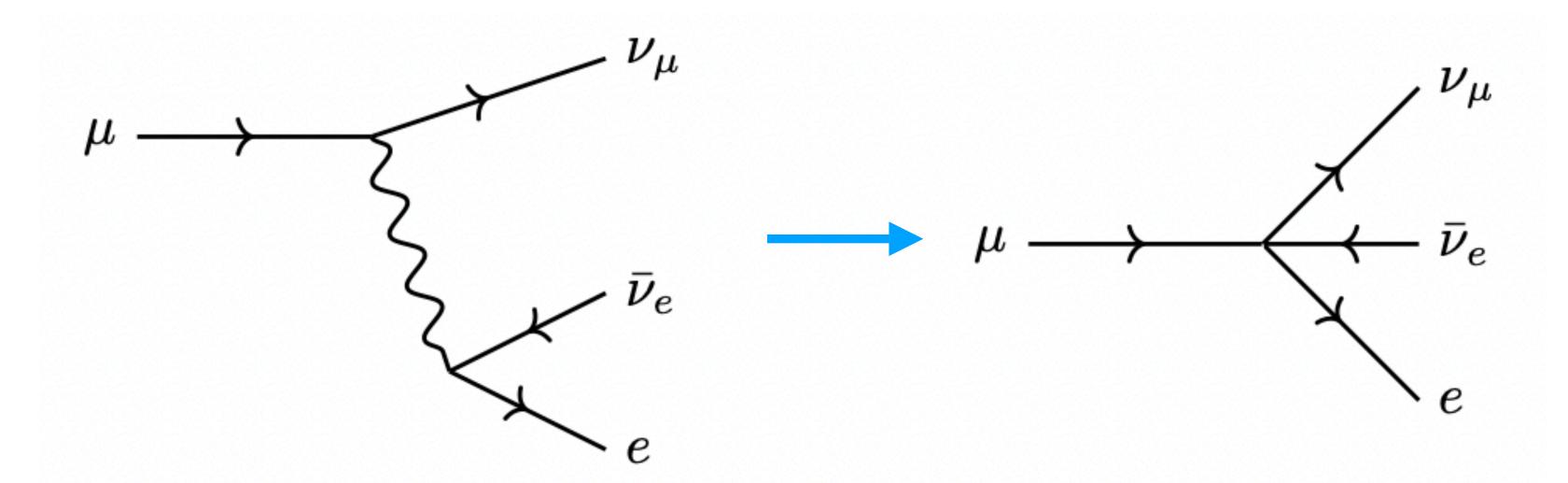
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- However, there are **thousands** of possibilities, so just guessing particles seems a bit like **stabbing in the dark**!
- Some models are **more motivated** than others, but it would be nice to have a more general approach...

• Fortunately, the language of **effective field theory** exists to help us tackle this problem.

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- Idea: at low energies we can integrate out heavy particles from a theory, giving effective non-renormalisable interactions:



Integrating out particles can also yield shifts in SM couplings.

Since any\* heavy particle manifests at low energies as non-renormalisable interactions, if we are hunting for extensions of the SM, we can simply add on all non-renormalisable operators built from the SM fields (and respecting the SM symmetries):

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• We can organise the additional non-renormalisable operators by their mass dimension, with higher-dimensional operators being suppressed by powers of  $1/\Lambda$ , where  $\Lambda$  is a characteristic scale of the New Physics.

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- However, the number of operators decreases significantly if we assume additional symmetries, e.g. no baryon number violation. There are only 59 operators if we assume flavour universality.
- The main sectors studied so far are: top, Higgs and electroweak physics.

$$\mathcal{L}_{SMFFT} = \mathcal{L}_{SM} + \mathcal{L}_5 + \mathcal{L}_6 + \cdots$$

• Finally, note that various fitting groups **just fit** the SMEFT couplings, for example the **SMEFiT collaboration**, and the **FitMaker collaboration**.

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- Finally, note that various fitting groups **just fit** the SMEFT couplings, for example the **SMEFiT collaboration**, and the **FitMaker collaboration**.
- In particular, SMEFiT and FitMaker both assume a **SM PDF input**. This could be **problematic** because the PDFs were fitted **assuming no New Physics**...

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#### PDF parameter fits

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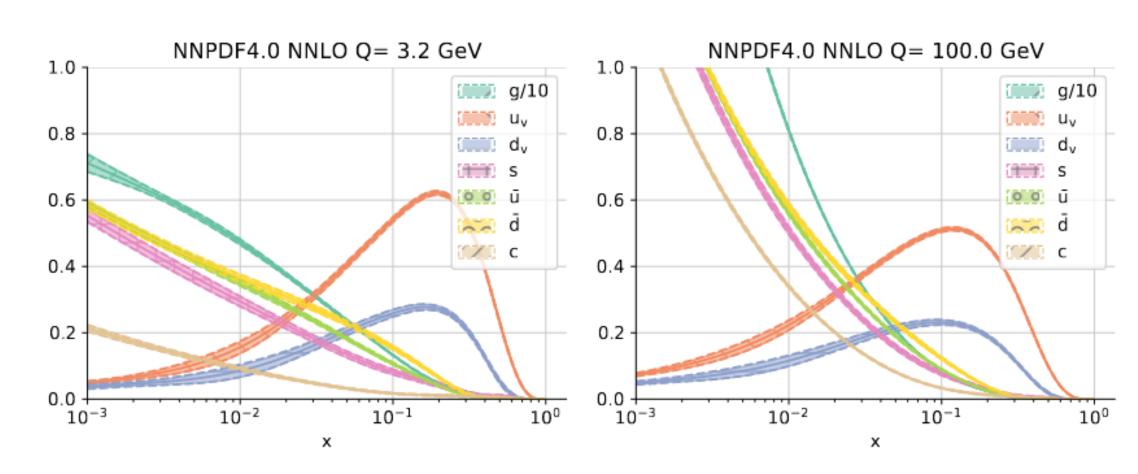
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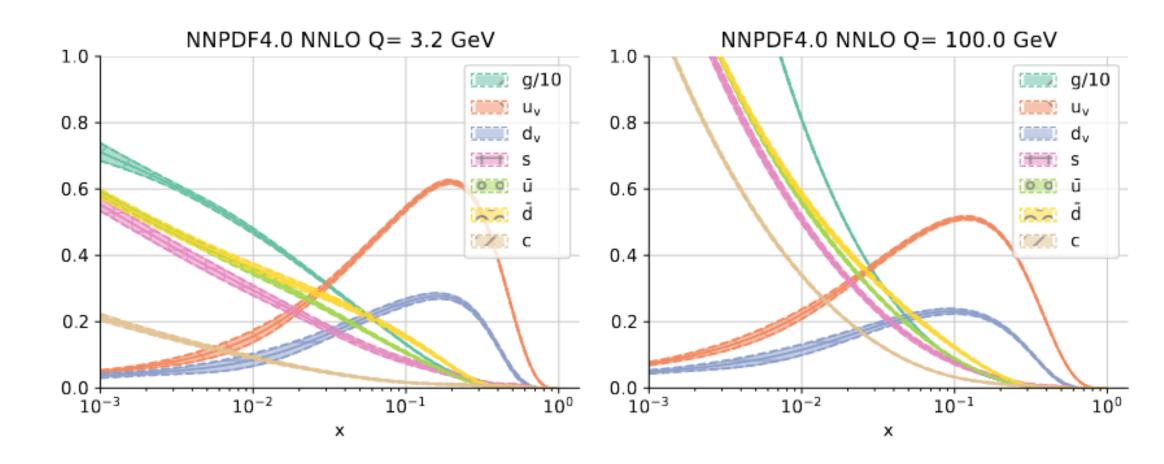
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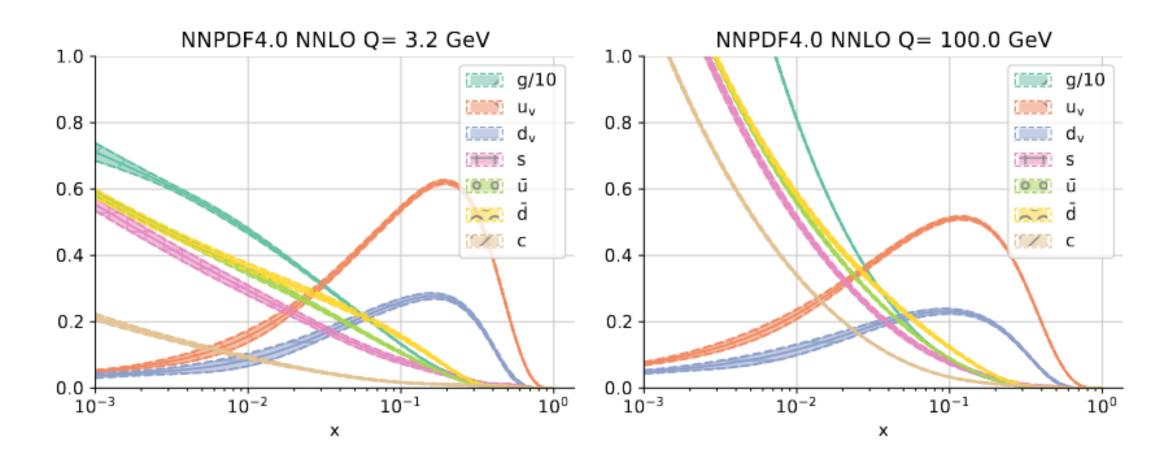
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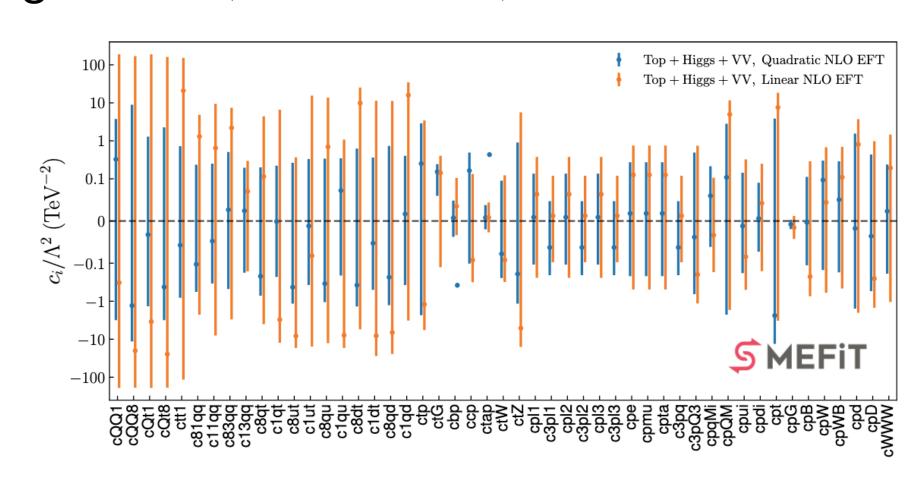


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- We could even miss New Physics, or see New Physics that isn't really there!

# Key question for remainder of section:

To what extent do bounds on SMEFT parameters change if they are fitted simultaneously with PDF parameters? Is a consistent treatment important?

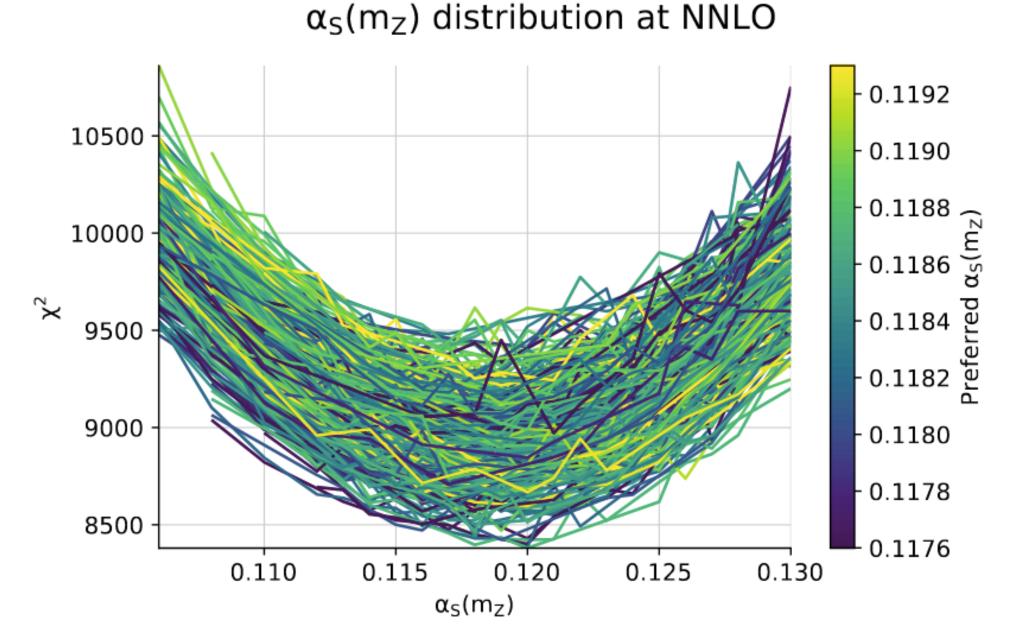
• This is not a new problem! It's been known for a while that simultaneous fits of SM parameters alongside PDFs can be important in many cases. In particular, PDF parameters have a strong correlation with the strong coupling  $\alpha_S(m_Z)$  (see e.g. Forte, Kassabov, 2001.04986).

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  - 3.  $\chi^2$  parabolas for each set of correlated replicas are produced, and hence bounds on  $\alpha_S(m_Z)$  are found.

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A proof-of-concept study, performing a simultaneous extraction of 4 four-fermion SMEFT operators together with PDFs, using DIS-only data.

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A methodological study; simultaneous SMEFT/ PDF extraction is noted as a possible application, and one SMEFT four-fermion operator is fitted using DIS-only data. 3. **PBSP team + Greljo and Rojo, 2104.02723**. Parton distributions in the SMEFT from high-energy Drell-Yan tails.

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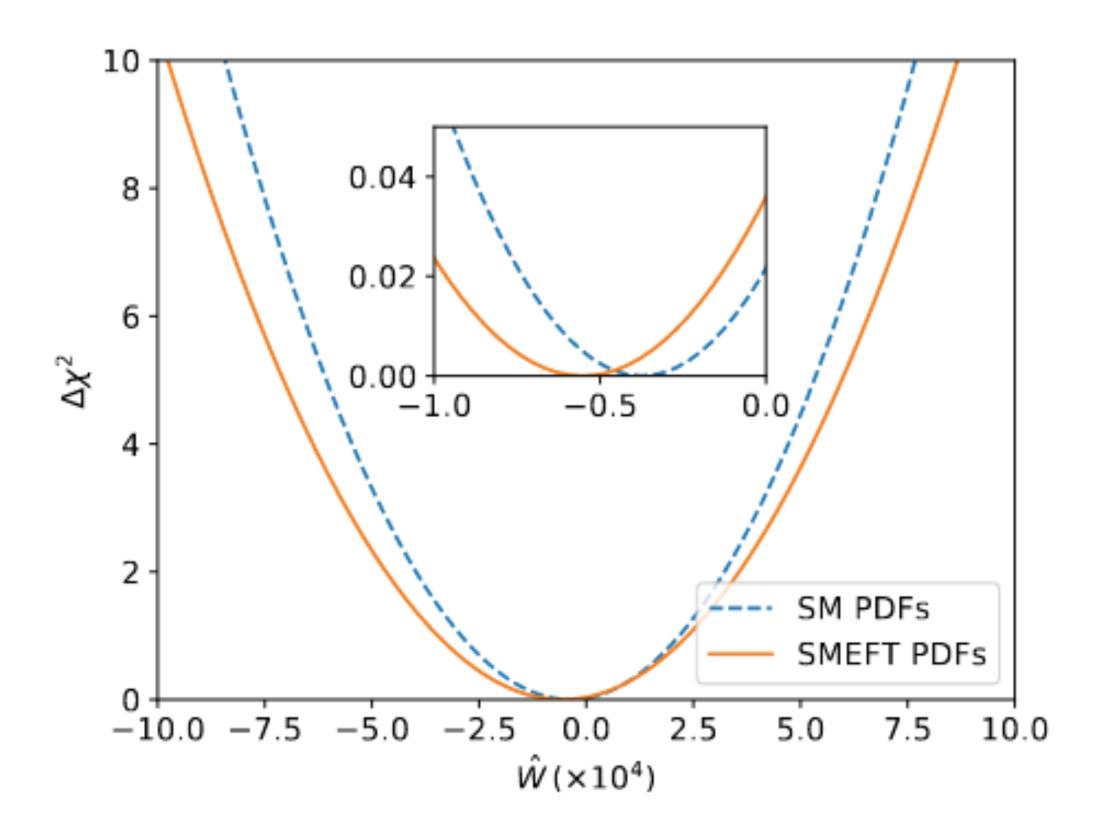
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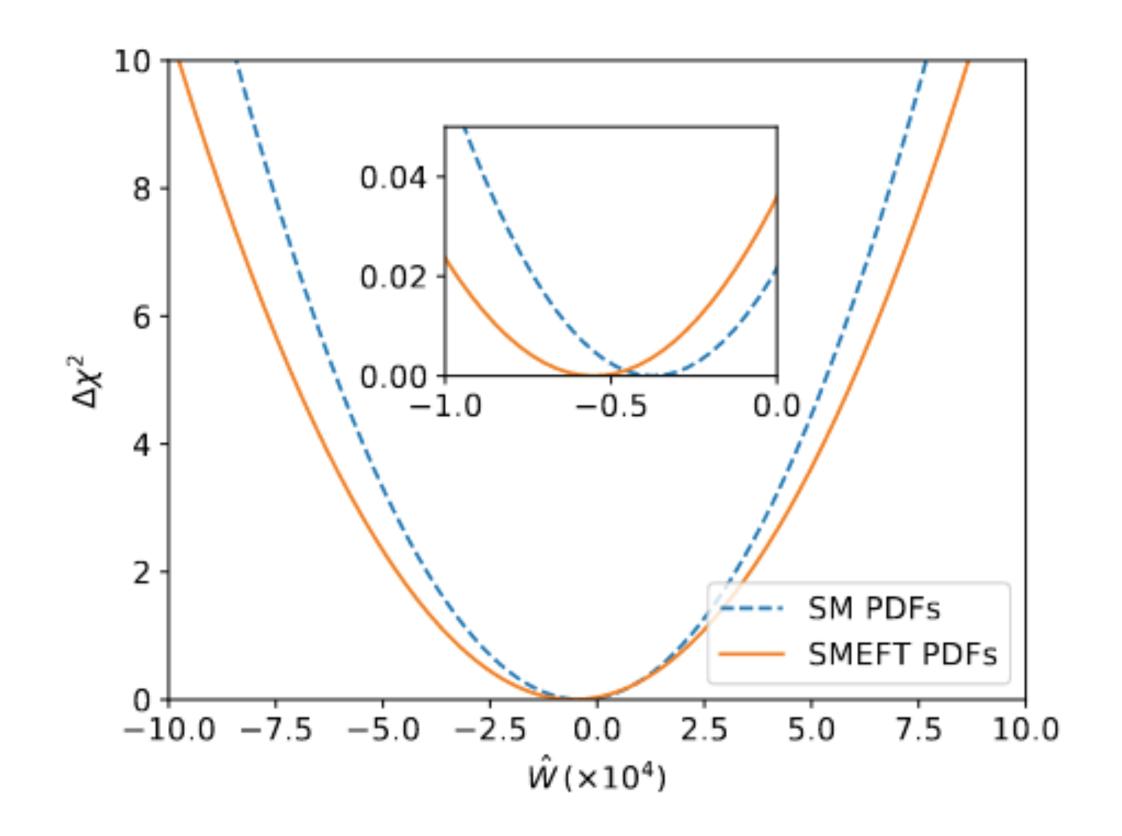
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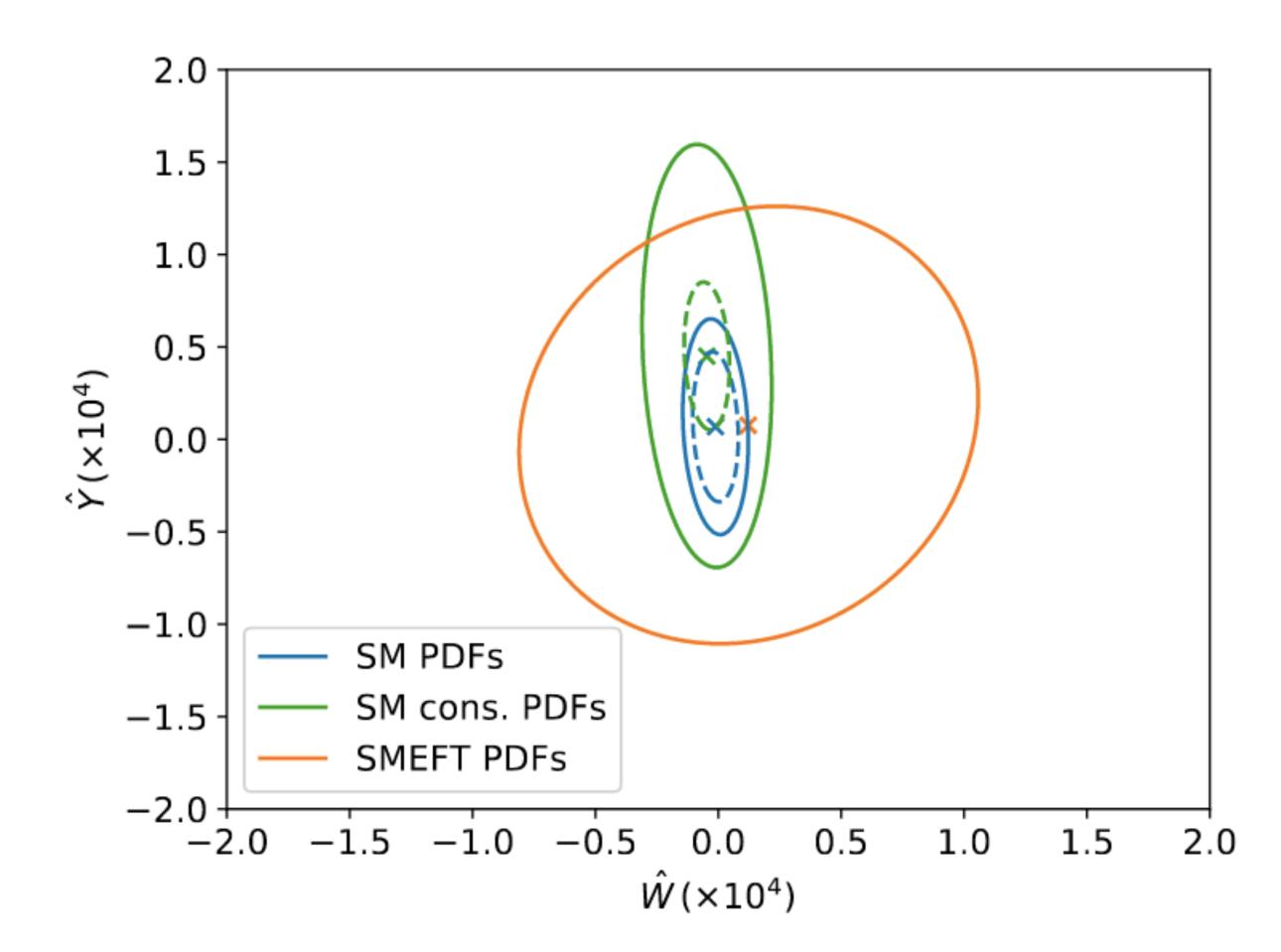


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- The methodology used is similar to the 'scan' methodology described for the  $\alpha_S(m_Z)$  fit, but replicas are not correlated, we simply take the  $\chi^2$  of a PDF fit at each benchmark point in Wilson coefficient space to construct bounds.



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- Without a simultaneous fit, we find that the size of the bounds is significantly underestimated - this could lead to claims of discovering New Physics when it isn't necessarily there.



 We have now seen the future need for simultaneous PDF-SMEFT extractions.

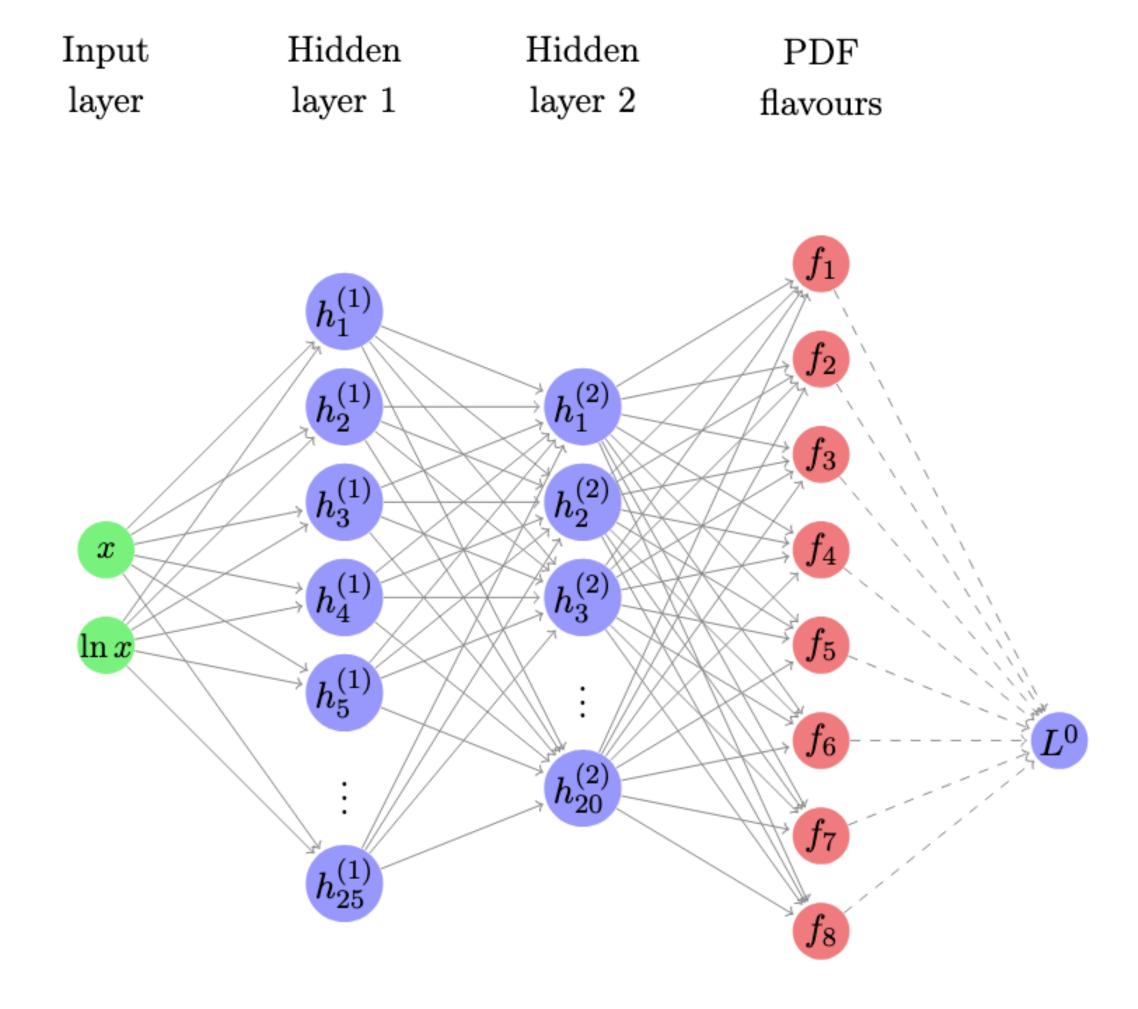
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- Two members of the PBSP group have developed another approach based directly on the NNPDF4.0 PDF-fitting framework, which we call the SimuNET methodology, presented in Iranipour, Ubiali, 2201.07240.

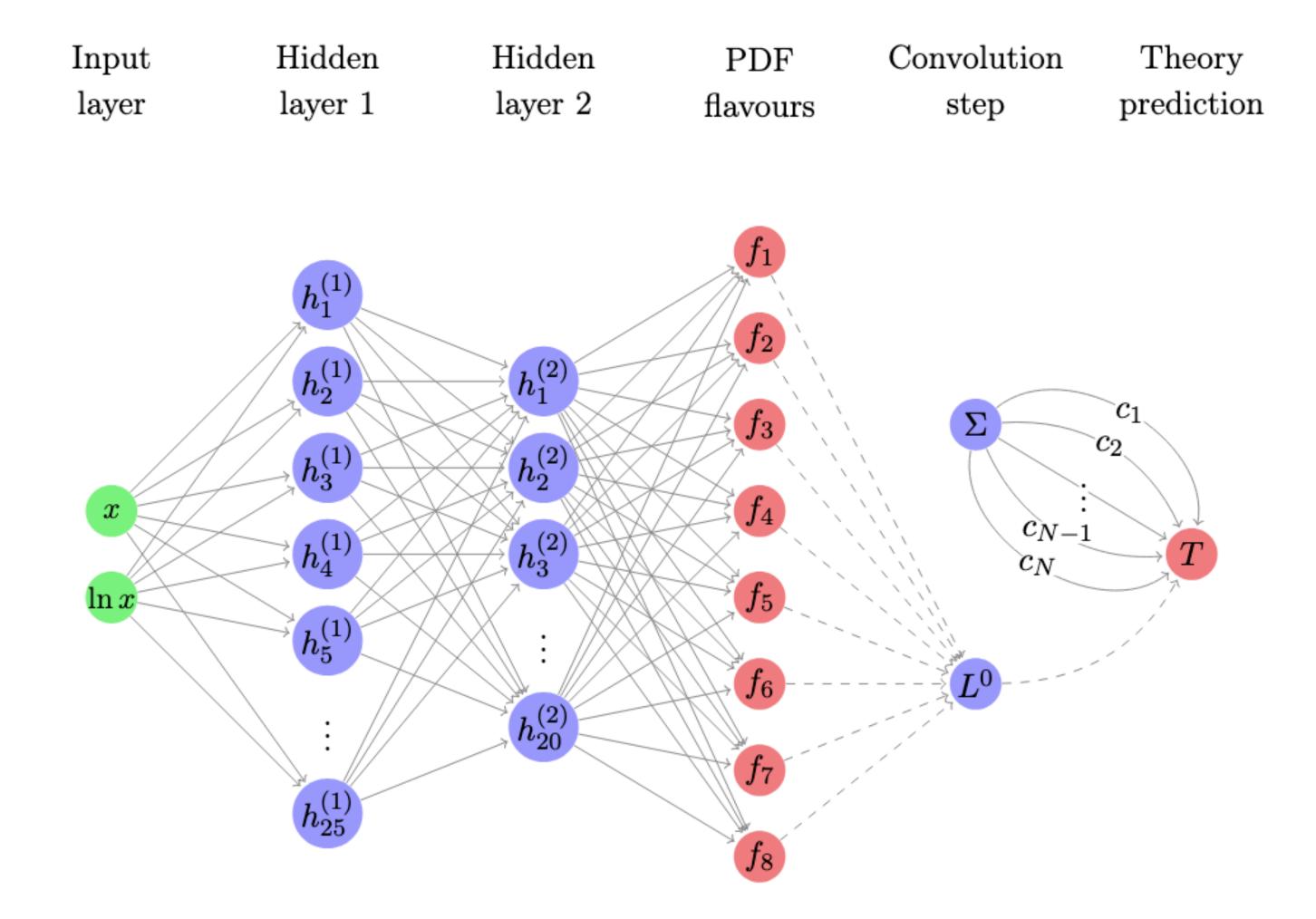
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- The SMEFT couplings are added as weights of neural network edges, and are trained alongside the PDFs.



#### Benchmark of results

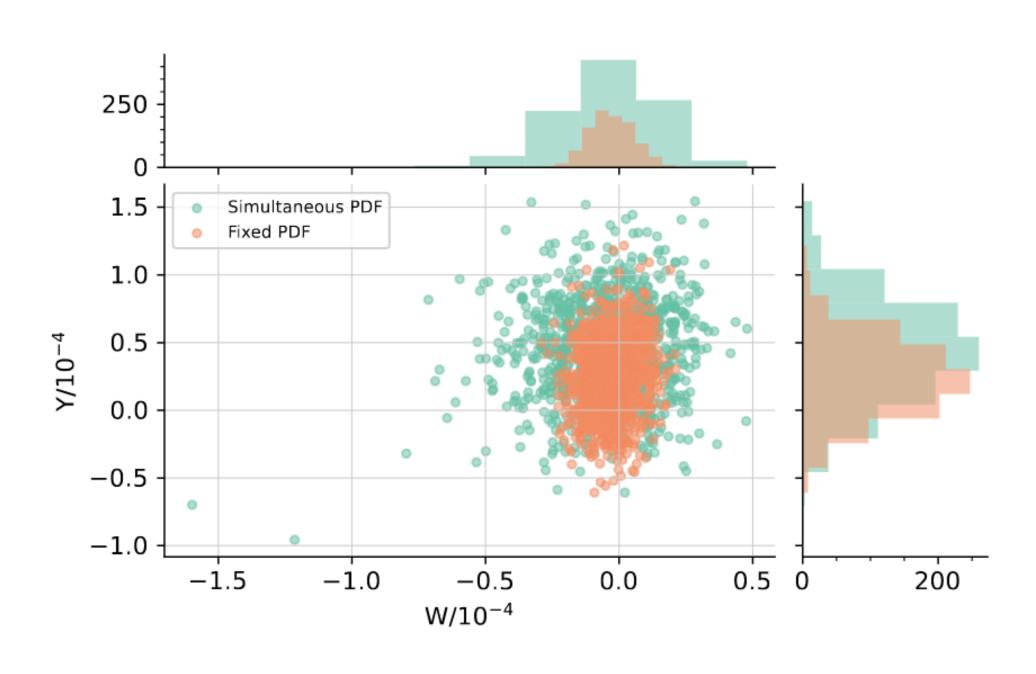
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- Compatible bounds in all cases are obtained, with similar broadenings of the bounds on the SMEFT couplings compared with fixed PDFs in the projected HL-LHC fit.

	SM PDFs	SMEFT PDFs	best-fit shift	broadening
$W \times 10^5$ (this work)	$\left[-2.0, 1.4\right]$	[-4.3,3.4]	-0.2	+126%
$W  imes 10^5 \; [17]$	[-1.4,1.2]	[-8.1, 10.6]	-1.4	+620%
$Y \times 10^5 (\mathrm{this\ work})$	[-3.2, 8.1]	[-3.1, 11.7]	+1.9	+31%
$Y \times 10^{5}[17]$	[-5.3, 6.3]	[-11.1, 12.6]	+0.3	+110%

Benchmark of bounds from SimuNET paper against Greljo et al., 2104.02723 ([17] in above)



#### Where next...?

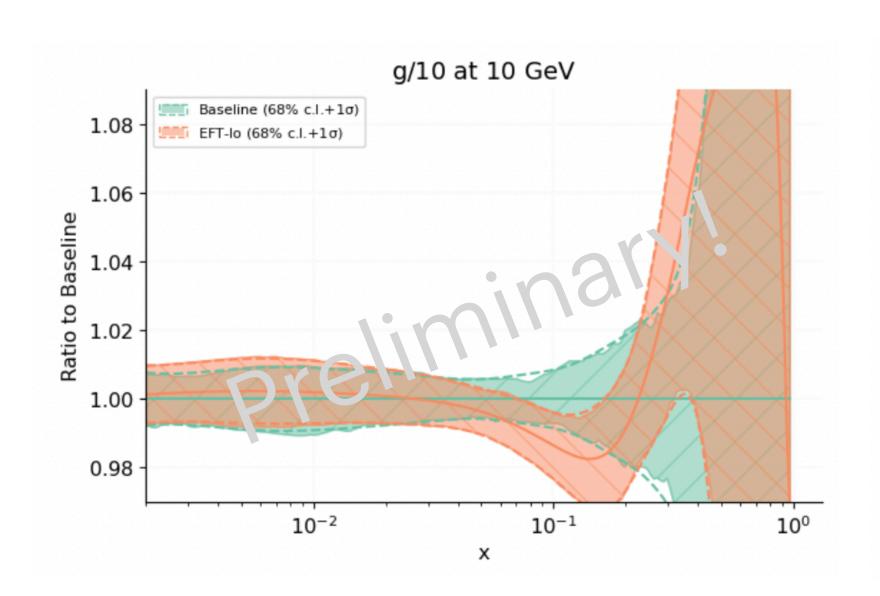
The PBSP group is currently working on a study applying the new SimuNET methodology to a joint PDF-SMEFT fit in the top sector. There are now 20 SMEFT couplings to fit alongside PDFs.

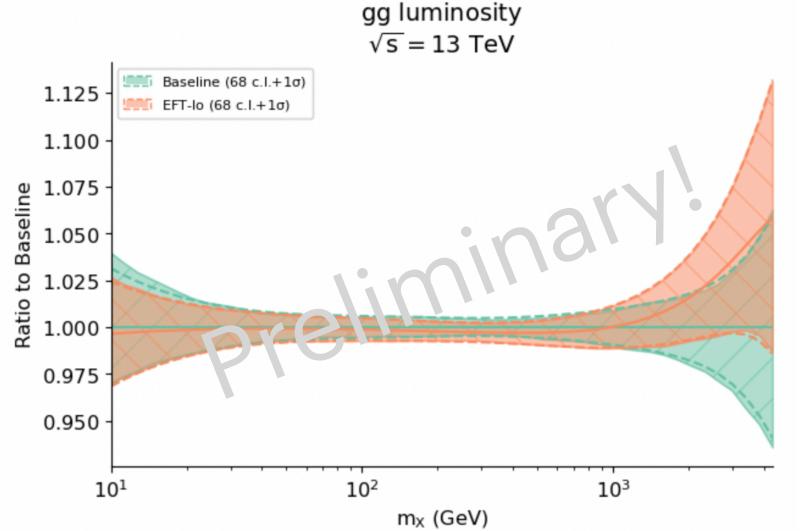
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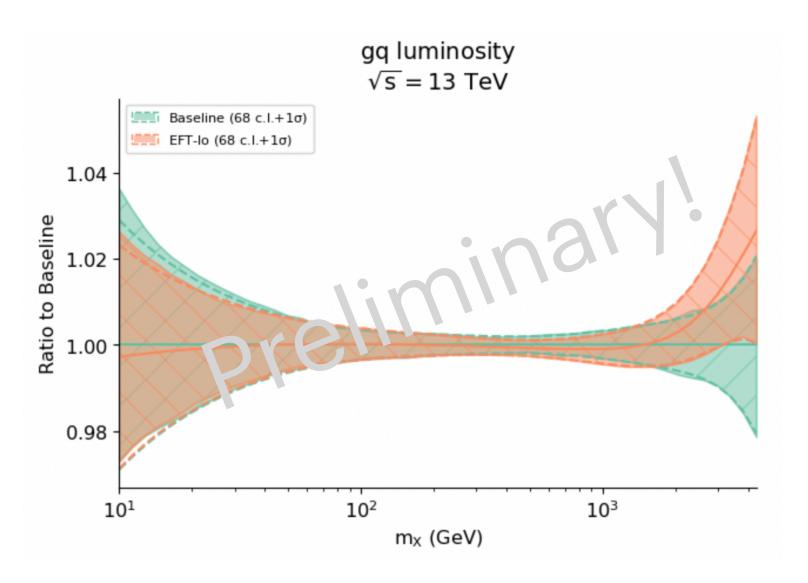
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- For PDFs, top data mainly impacts the gluon PDF at large x.
- Preliminary results show that simultaneously fitting SMEFT alongside PDFs can result in an enhancement in the gluon shift:







# 4. - The dark side of the proton

 So far, we've focussed on joint PDF-SMEFT determinations. However, whilst the SMEFT is a great tool in searching for New Physics, it does not capture new weakly-coupled, light particles. Proton structure could also be affected by these new degrees of freedom!

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- In this case, we could **still see the impact on proton structure** by including the new particles as **constituents of the proton**.
- The idea is not too far-fetched! The inclusion of new coloured particles, e.g. gluinos, has already been studied by Berger et al. in 0406143 (from 2005) and 1010.4315 (from 2010). Strong constraints can be derived assuming that new coloured particles alter our SM view of proton structure.

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- In McCullough, **Moore**, Ubiali, 2203.12628, we studied the impact of using a **toy dark matter candidate**, namely a **light leptophobic dark photon** B which couples to quarks via the effective interaction Lagrangian:

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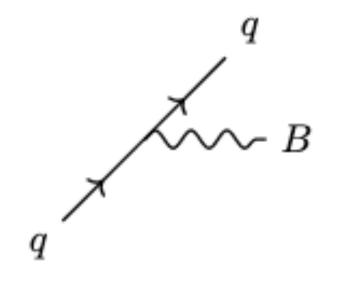
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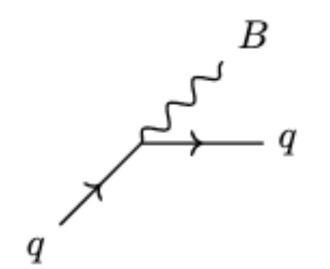
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- We also treat this as an effective theory, valid up to the mass of the Z, where **kinetic mixing** effects become important; so for us:  $m_R \in [2,80]$  GeV.

 Now, to include the dark photon as a constituent of the proton, we mimic the earliest studies into **photon PDFs** (namely MRST 0411040, from 2004), using the following procedure:

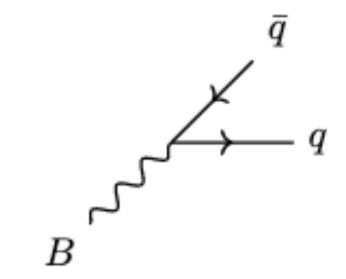
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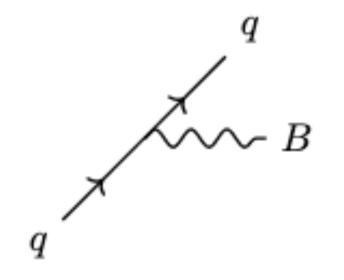


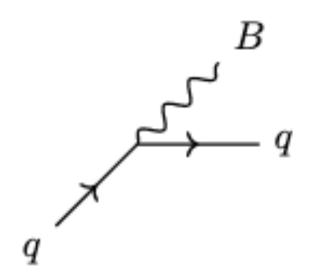
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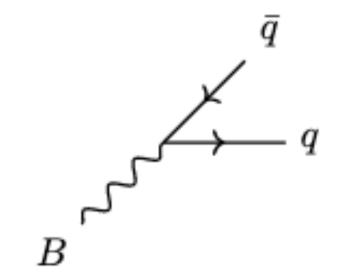
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  - Starting from an appropriate initial-scale ansatz, and a reference PDF set, evolve using the modified DGLAP equations. Since we assume  $m_R > 2\,$  GeV, greater than the standard initial scale 1.65 GeV, we always generate the dark photon from zero similar to a heavy quark. We choose the state-of-the-art NNPDF3.1 LUXQED set as our reference set (this will soon be replaced by NNPDF4.0 LUXQED).





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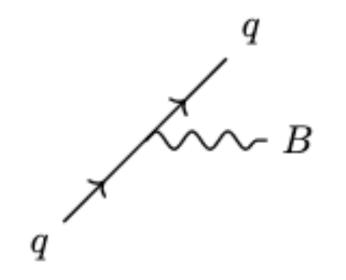


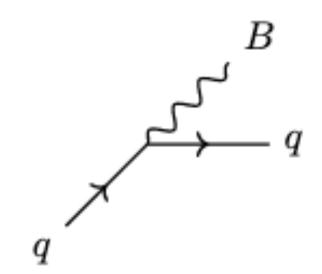
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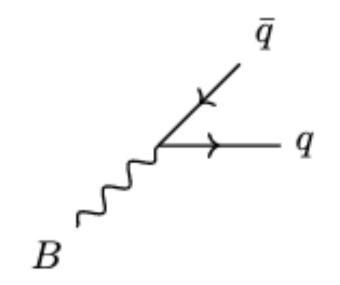
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  - Compare resulting PDF set predictions with reference SM predictions to see impact of inclusion of a dark photon.





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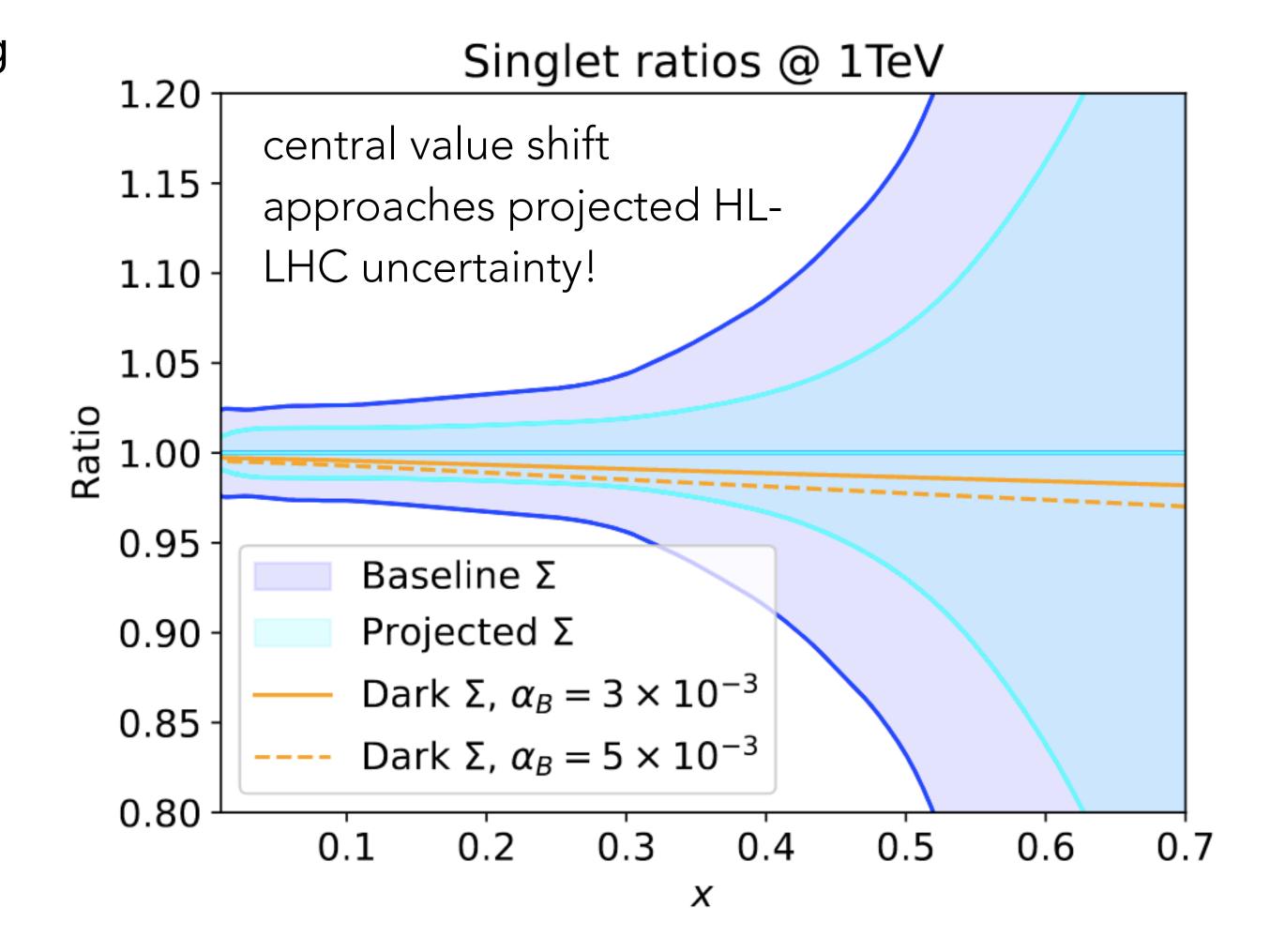
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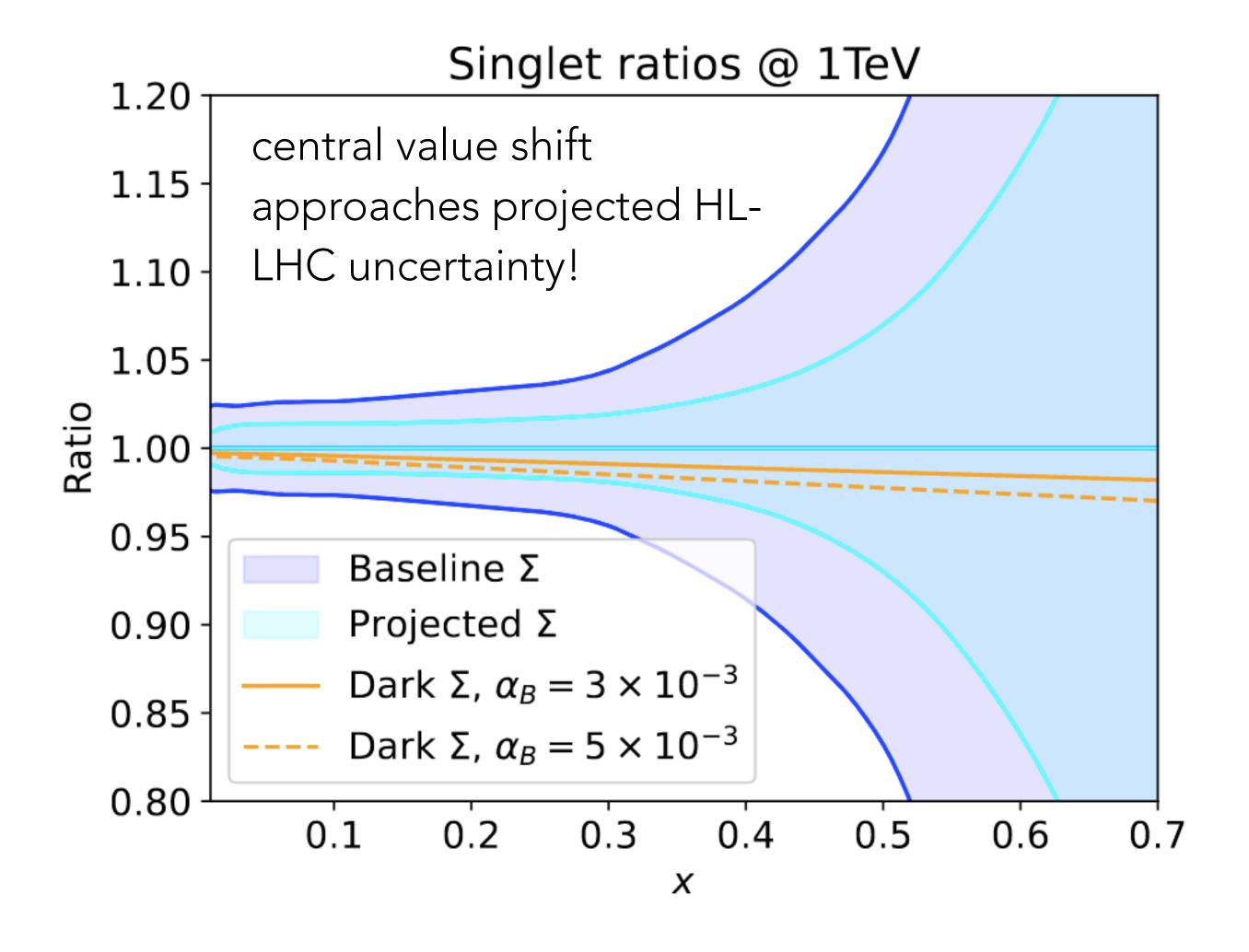
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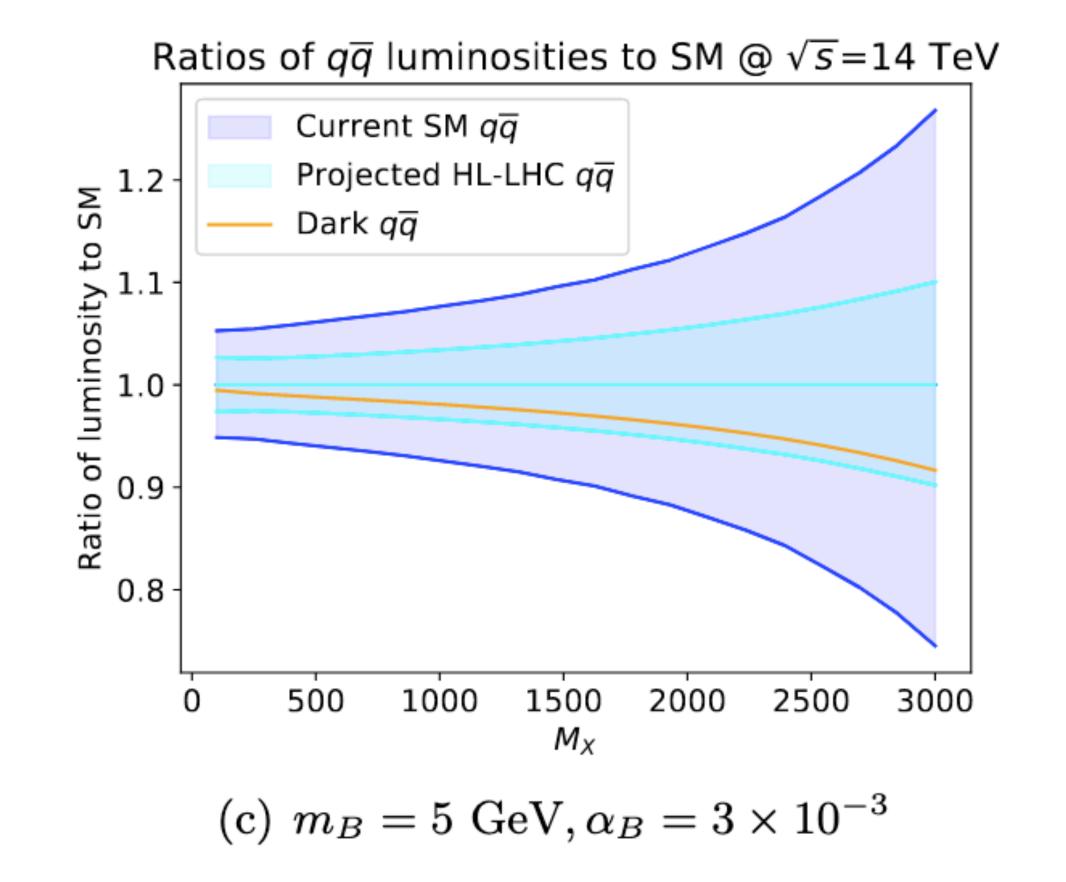
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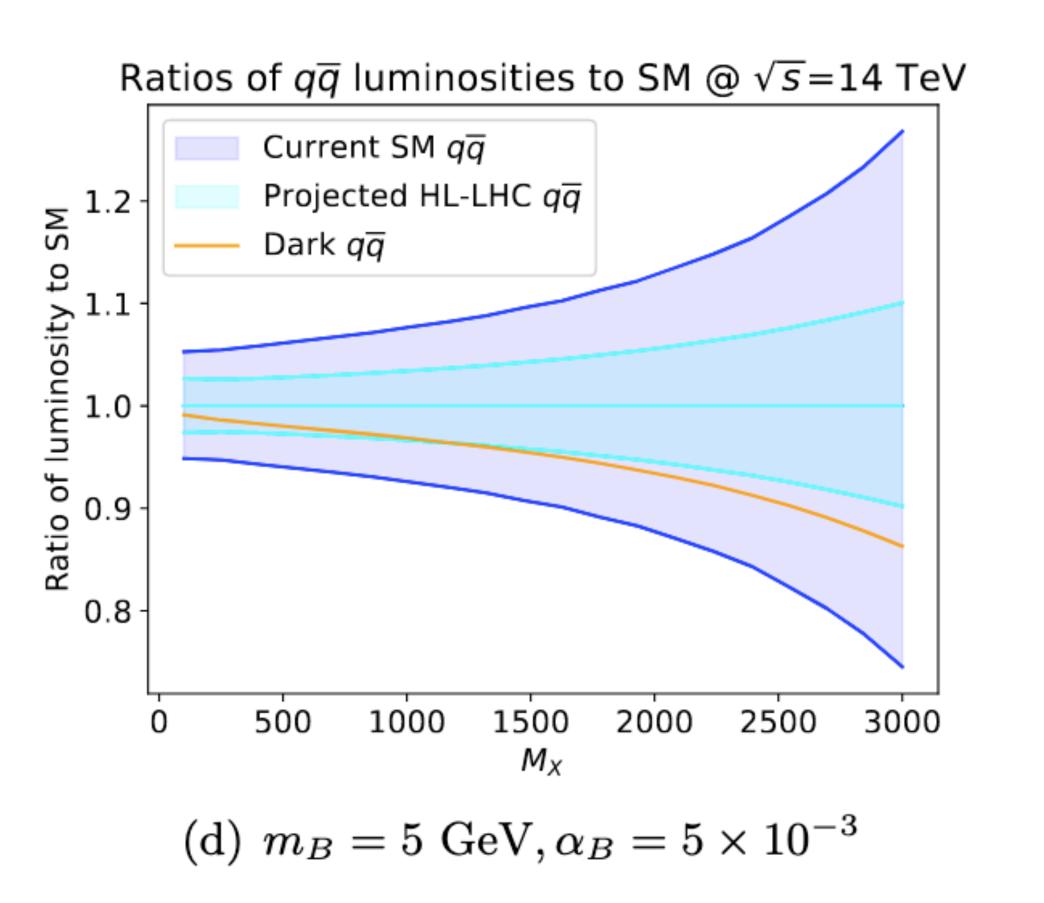


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- E.g. including a dark photon modifies the **singlet PDF**, as shown on the right. Light blue bands correspond to **projected PDF** uncertainty at the **HL-LHC** (see 1810.03639).
- The region that is most modified suggests that some values of the dark mass and coupling might lead to PDF sets which perform too poorly on Drell-Yan sets, relative to the baseline.



• The most important luminosity channel for DY is  $q\bar{q}$ ; here, there is **tension** with projected HL-LHC uncertainties for some values of the mass and couplings!





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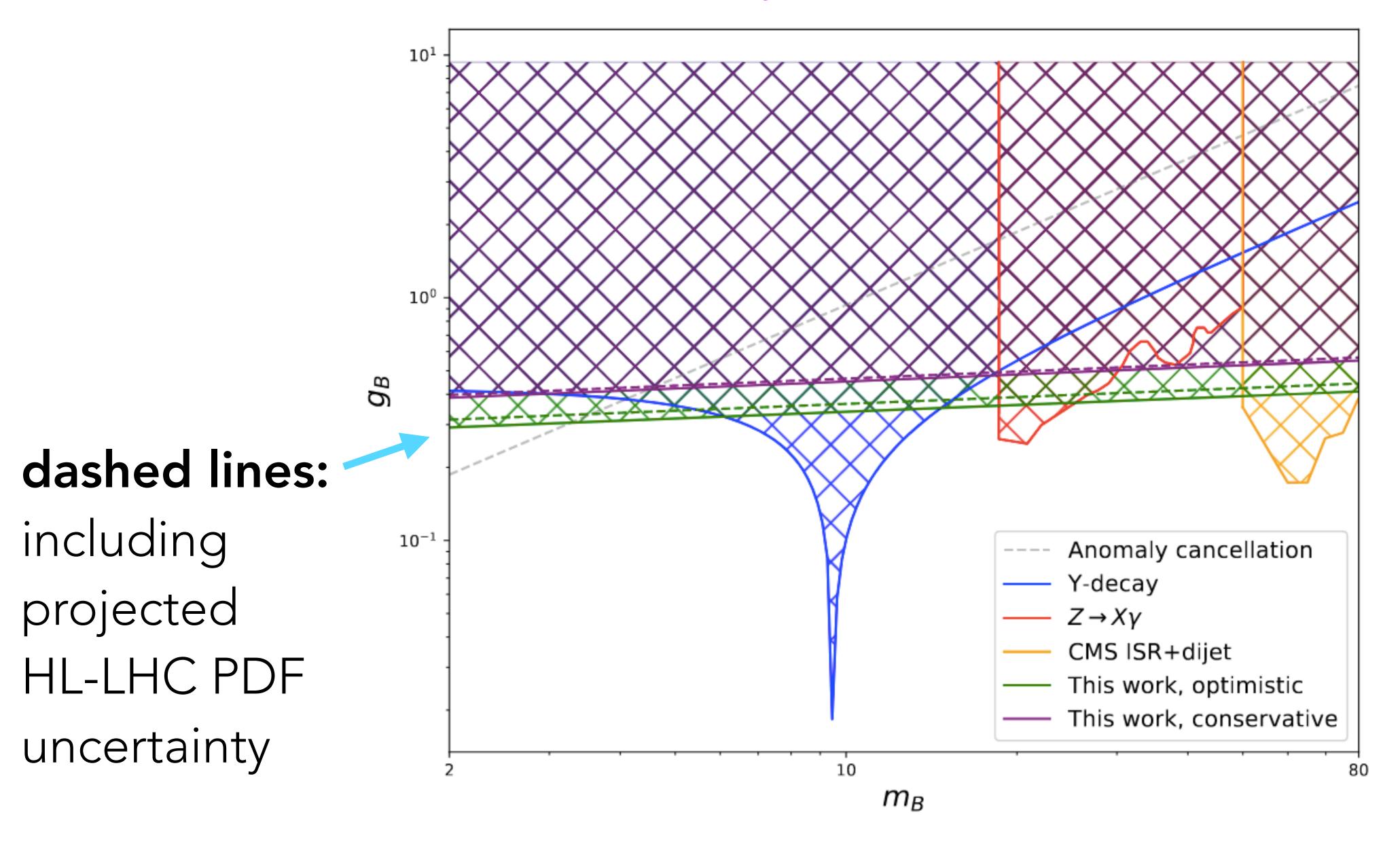
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  - 3. Compare to the reference fit's  $\chi^2$ -statistic, and hence obtain projected bounds.

• The specific HL-LHC observable we choose to use is **neutral current Drell-Yan** at a centre-of-mass-energy  $\sqrt{s}=14$  TeV, in 12 bins of lepton invariant pair-mass. The projected data we use is a small modification of that produced for **Parton Distributions in the SMEFT from High-Energy Drell-Yan Tails**, 2104.02723.

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### Comparison of (projected) bounds



## Conclusions

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• Simultaneous determination of PDFs and BSM parameters, will be very important in future analyses (especially as we enter Run III).

Members of the PBSP team have already produced two works in the direction of simultaneous PDF-SMEFT fits: (i) a phenomenological study 2104.02723 showing the need for simultaneous extraction; (ii) a methodology (SimuNET, 2201.07240) capable of fast simultaneous fitting. We aim to continue with a more ambitious top-sector fit.

• There are interesting directions outside the SMEFT, e.g. studying **light**, weakly-coupled particles inside the proton, like our dark photon study.

# Thanks for listening! Questions?